

Statistical Considerations in Setting Acceptance Criteria

1. Reference intervals (and outlier tests)
2. Tolerance intervals
3. Process performance indices, 6 sigmas, ...
4. Summary

Disclaimer

The views expressed here are those of the author and may not necessary reflect those of the German Regulatory Authorities



Reference Intervals

- Mean $\pm$ 2 standard deviations (Mean $\pm$ 3 s)
- Easy to implement
- Data should be symmetrically (ideal: normally) distributed
- Otherwise: Transformation of the data
- Reliable, unbiased estimation of mean and standard deviation necessary

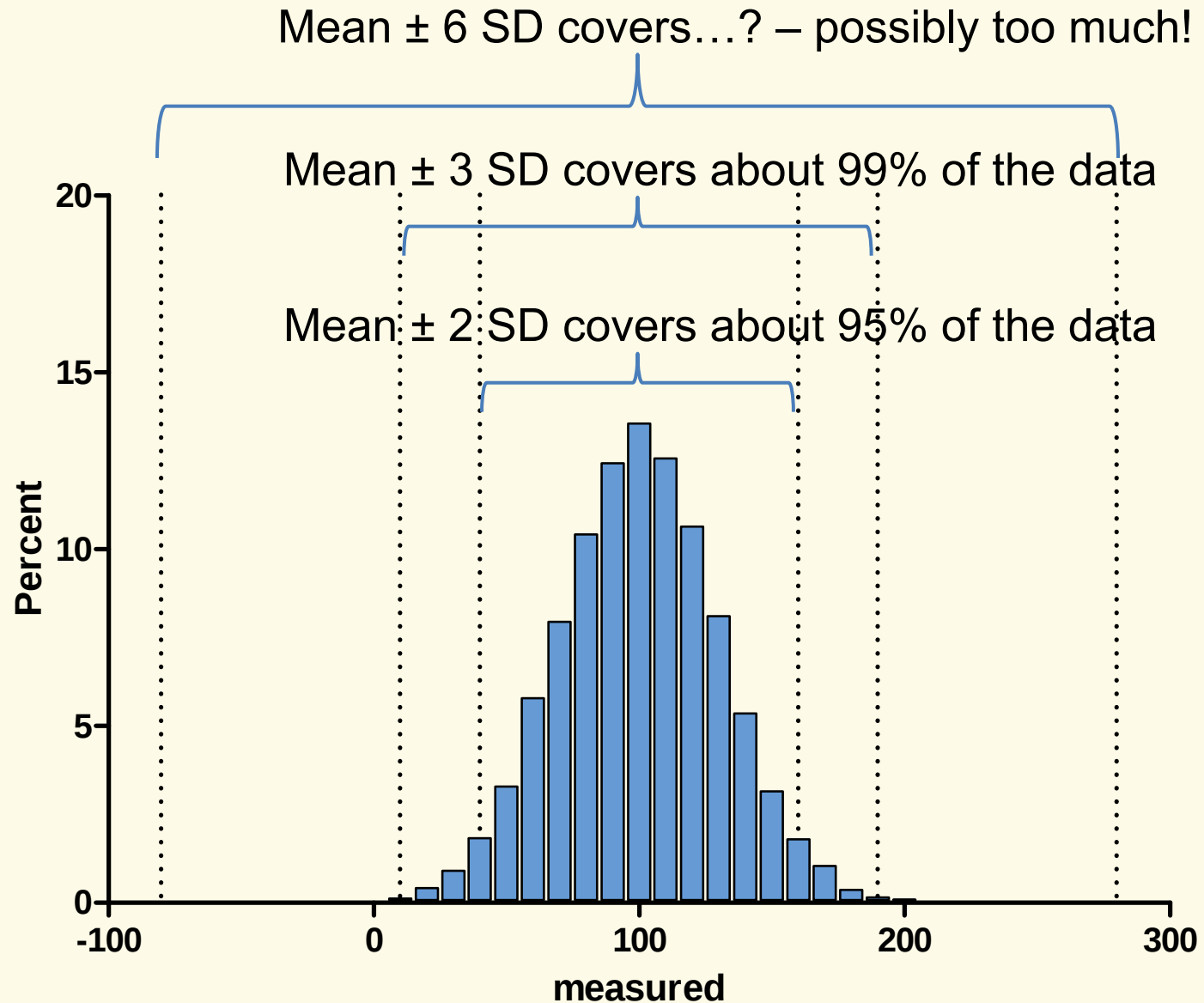
1-2-3- σ -Rule

Reference Intervals include a certain amount of the data
(assumption: normal distribution)

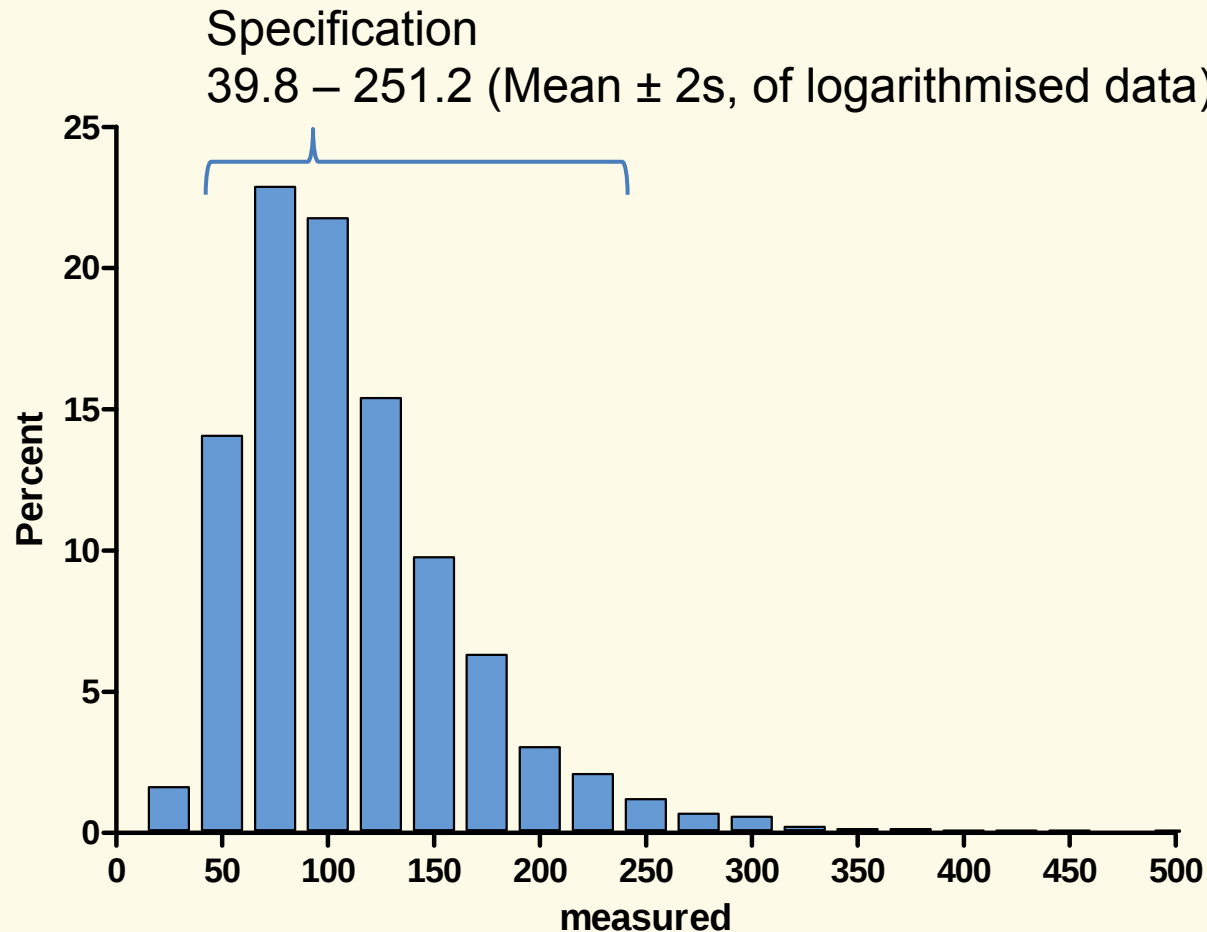
Interval	Probability	
	Within	Outside
Mean $\pm$...		
... 1 s	0.683	0.317
... 2 s	0.954	0.046
... 3 s	0.998	0.003
... 1.64 s	0.900	0.100
... 1.96 s	0.950	0.050
... 2.58 s	0.990	0.010

95% of the data can be found in the interval [Mean - 2 s, Mean + 2s]

Or: With 95% probability a value lies in this interval



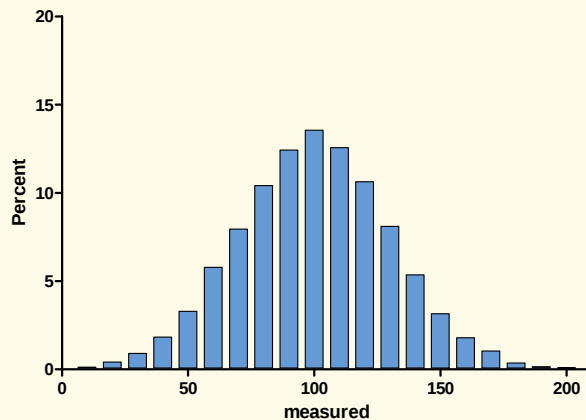
Skewed distributions / non-normal distributed data: Transformation of data (→ skewed specification)



How much data needed to set up specifications?

Simulated with true population parameters: $\mu = 100$, $\sigma = 30$

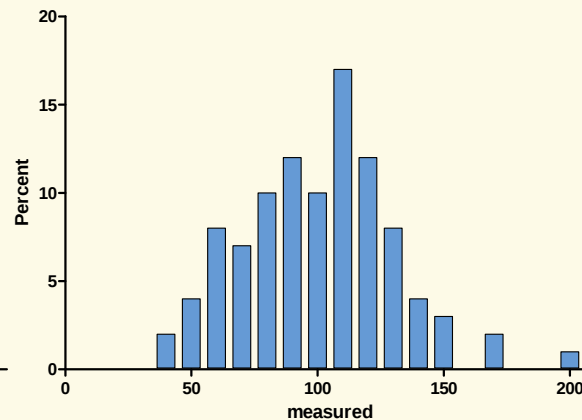
N=10,000



95%-Confidence
Interval

$\bar{x} = 99.9$ [99.3 – 100.5]
 $s = 30.0$ [29.6 – 30.4]

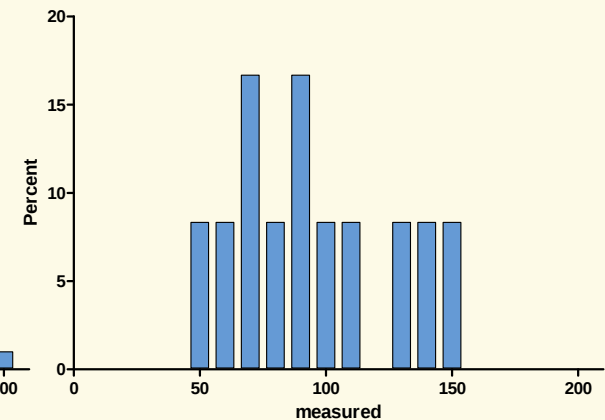
N=100



95%-Confidence
Interval

$\bar{x} = 100.9$ [95.0 – 106.8]
 $s = 29.9$ [26.3 – 34.8]

N=12

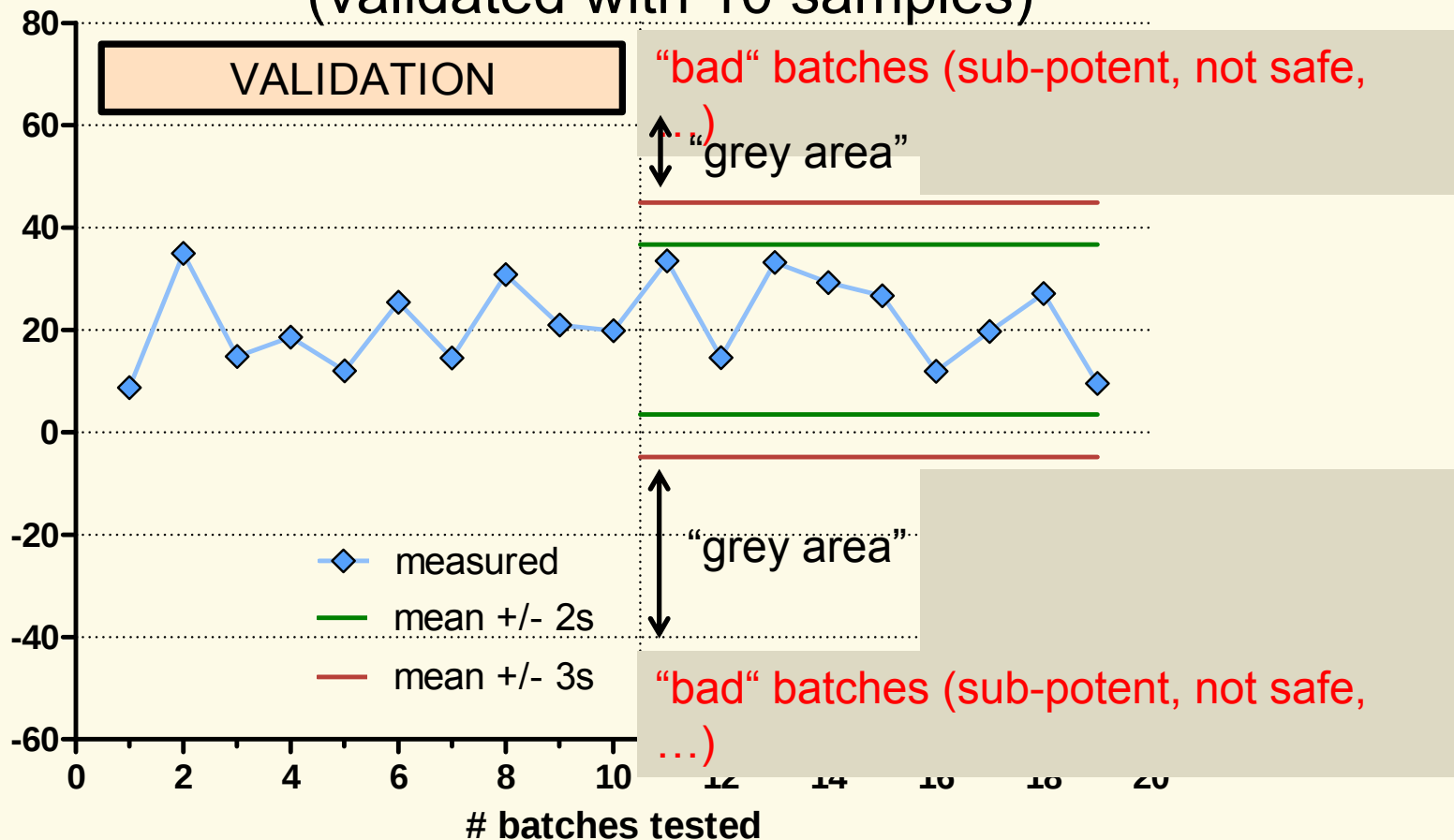


95%-Confidence
Interval

$\bar{x} = 96.2$ [76.6 – 115.8]
 $s = 30.9$ [21.9 – 52.5]

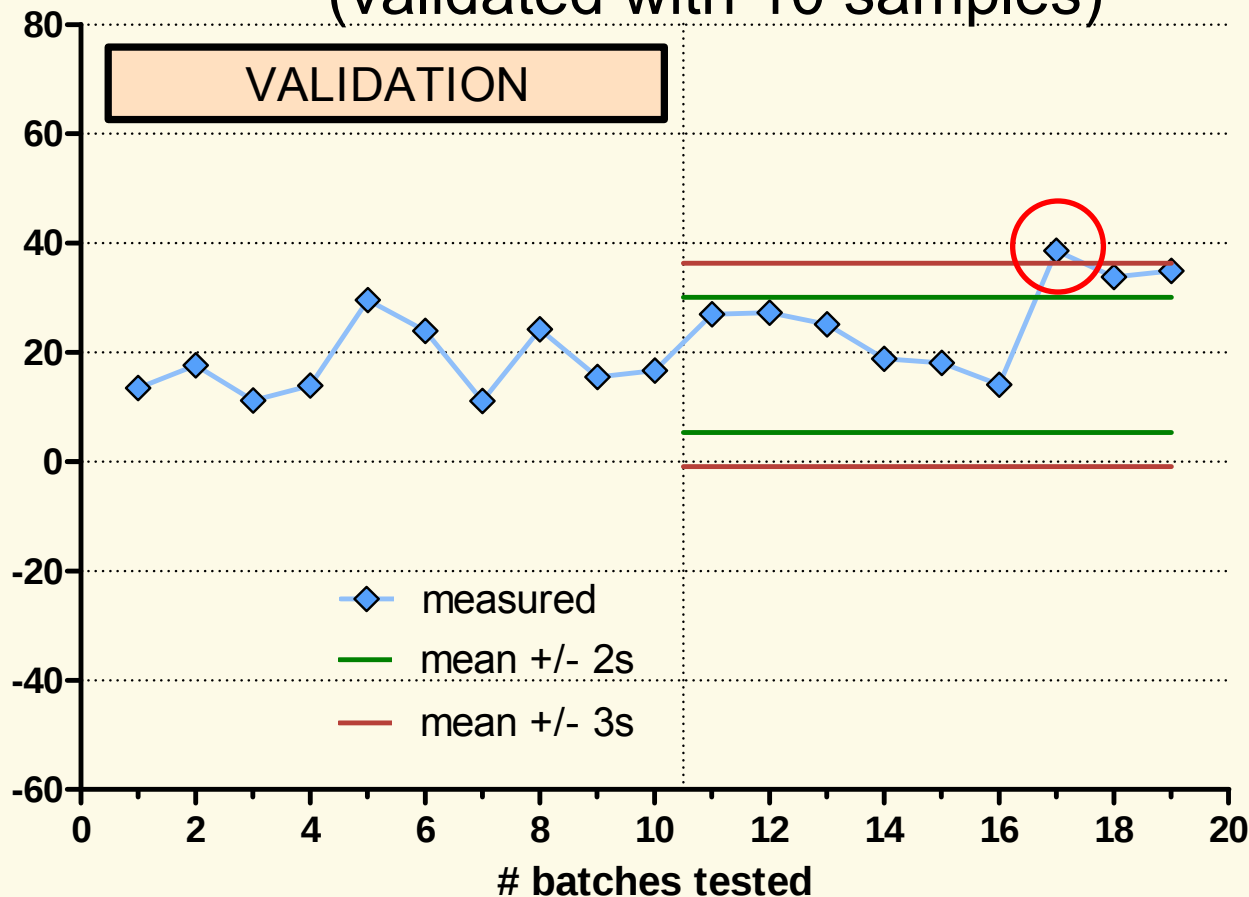
Example Reference Interval I

Mean $\pm 2s$ as “warning” limits,
Mean $\pm 3s$ as “intervention” limits
(validated with 10 samples)



Example Reference Interval II

Mean $\pm 2s$ as “warning” limits,
Mean $\pm 3s$ as “intervention” limits
(validated with 10 samples)



Outliers and outlier tests

Is it an outlier? – Or does it belong to the population?

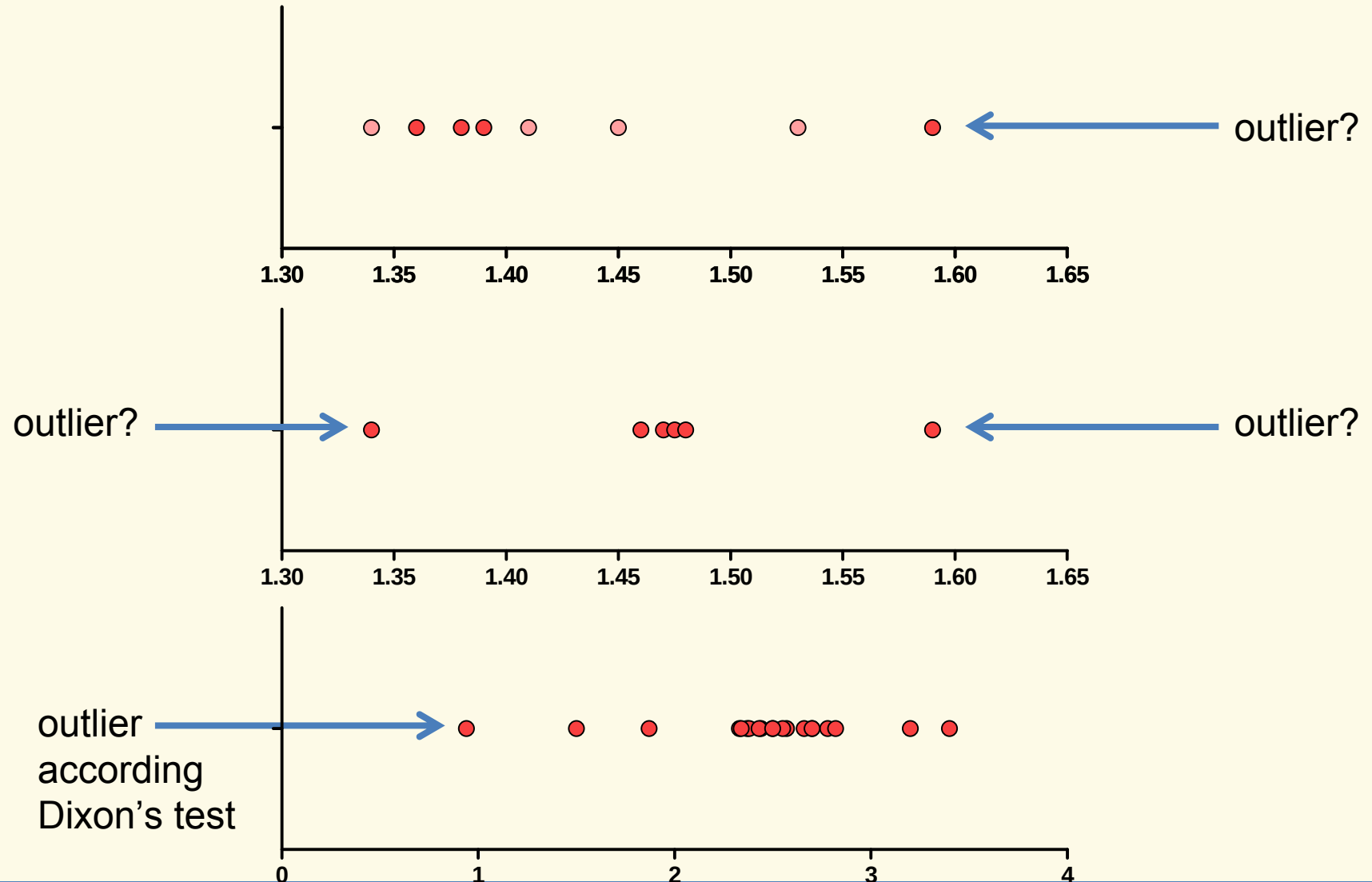


Torere, Bay of Plenty, New Zealand

It depends on how much information we have...

1. Outlier tests

There are several outlier tests... but be careful using them!



Tolerance Intervals

Intervals that cover percentiles of the population with a certain probability

Non-parametric TI – percentiles:

- Example: $[p_{0.05} - p_{0.95}]$ might serve as TI for the mean 90% of the population
- Example: Smallest – largest observation $[y_{(1)} - y_{(n)}]$ might serve as TI for whole population
- BUT: To cover actually 90% of the population with $[y_{(1)} - y_{(n)}]$, $N=19$ measurements are necessary
- AND: To cover actually 90% of the population with $[y_{(1)} - y_{(n)}]$ with 95% probability, $N=46$ measurements are necessary

TI (2–sided) for normal distributed data:

$$\bar{x} \pm k_{n;\gamma} s$$

with

$\bar{x}$ as mean of validation samples,

s as standard deviation,

n as number of samples tested,

γ as proportion of population covered, and

$$k_{n;\gamma} = \sqrt{\frac{n+1}{n}} t_{n-1; \frac{1+\gamma}{2}}$$

(t : quantile of t distribution)

This TI covers γ (%) of the population

Guttman (1970), Rasch (1996)

TI (2–sided) for normal distributed data:

$$\bar{x} \pm k_2 s$$

with

$\bar{x}$ as mean of validation samples,

s as standard deviation,

n as number of samples tested,

γ as proportion of population covered,

p as probability for $\gamma\%$ coverage (tolerance level), and

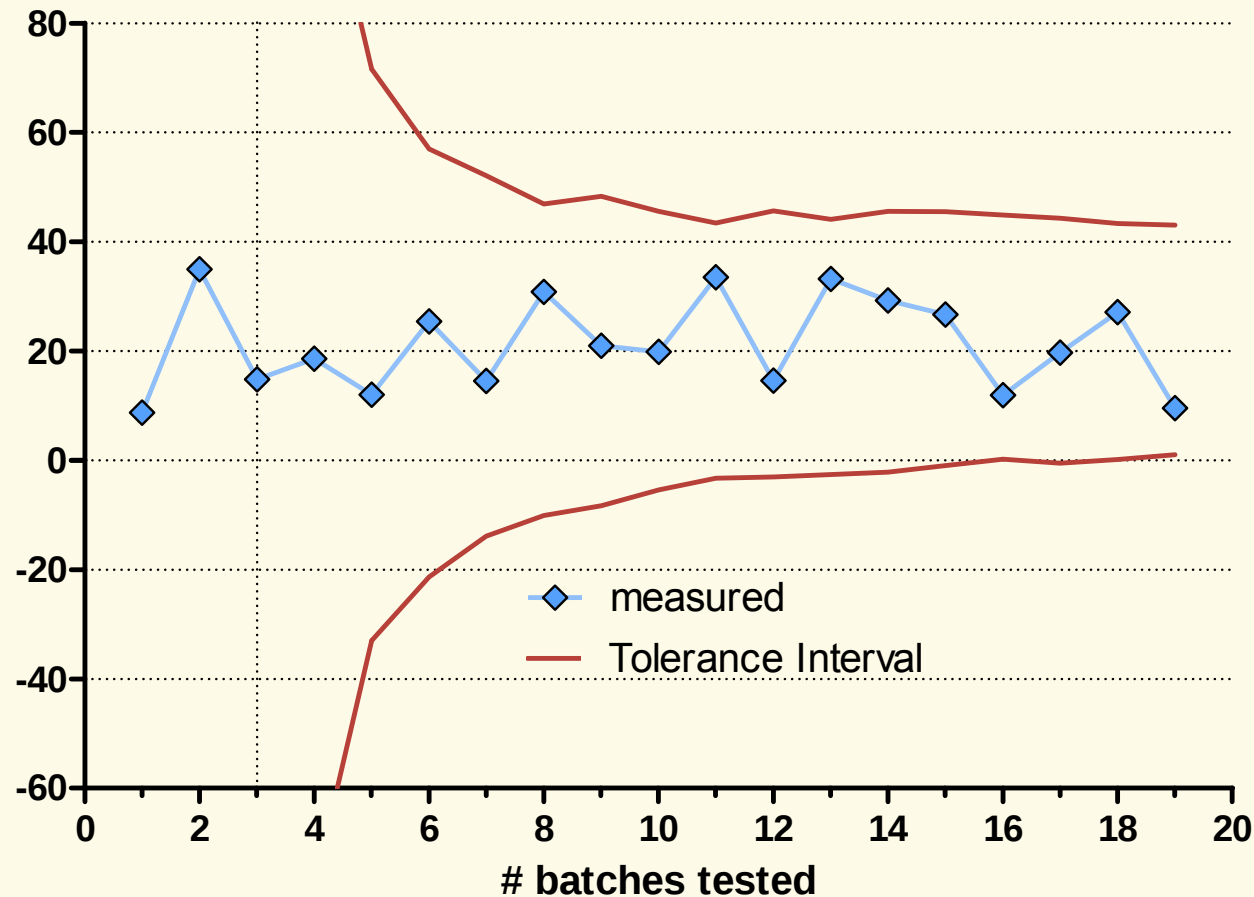
$$k_2 = \sqrt{(n-1) \left(1 + \frac{1}{n}\right) z^2_{(1-p)/2} / \chi^2_{\gamma; n-1}}$$

(z : quantile of normal distribution and
 χ^2 : quantile of χ^2 -square distribution)

This TI covers γ (%) of the population with probability p (%)

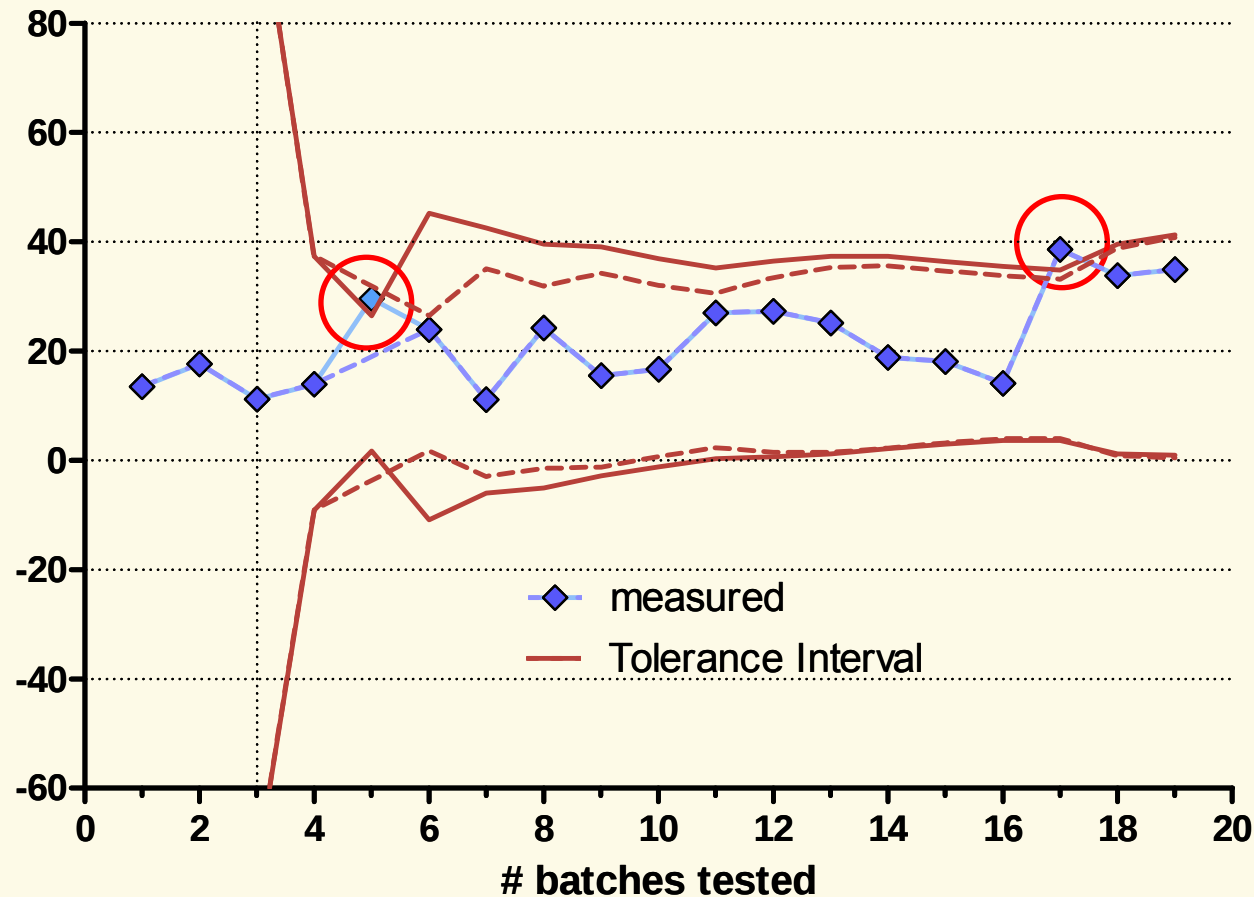
Howe (1969)

Dynamic Tolerance Intervals
($\gamma=0.95$, $p=0.95$; repeatedly calculated for $n \geq 2$ observations)



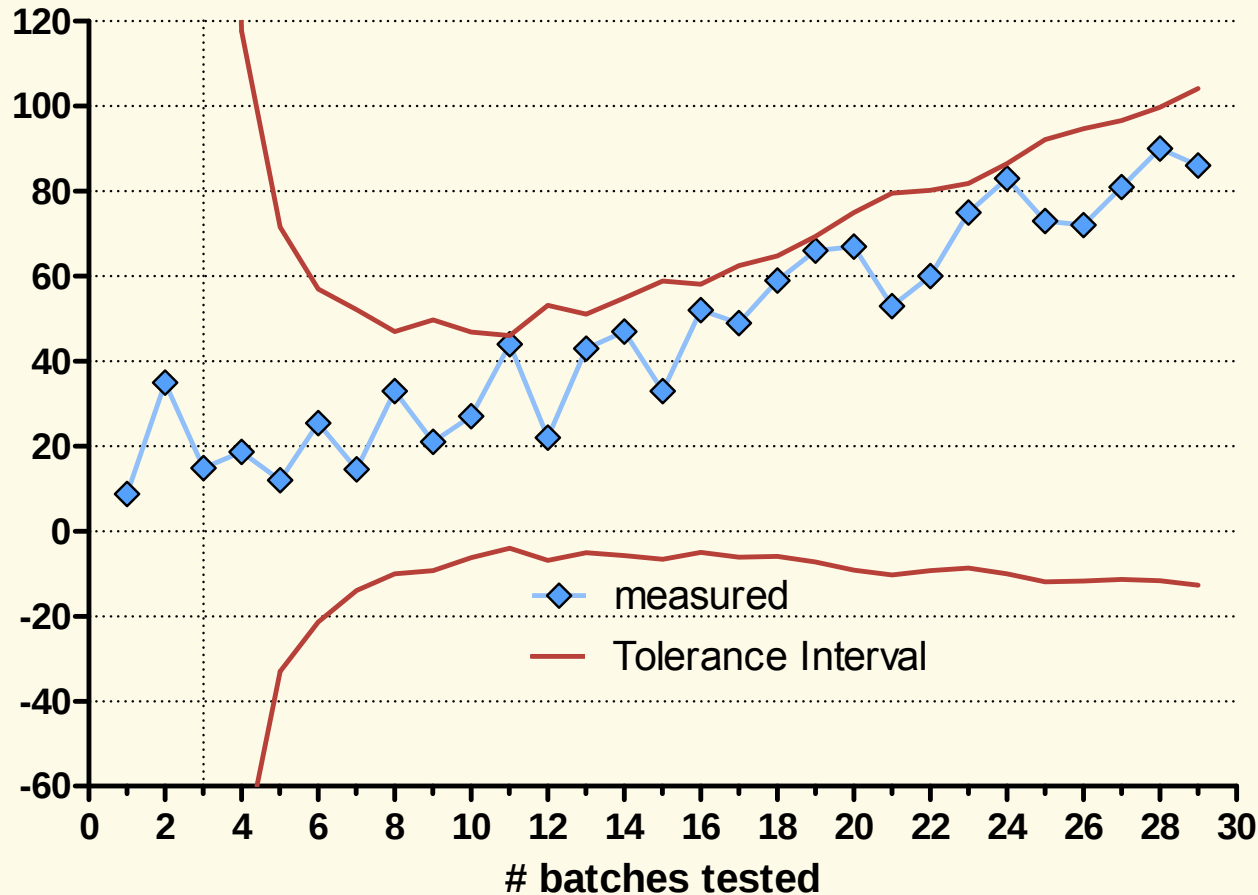
Dynamic Tolerance Intervals

What about early OOS results? May belong to population – or may be OOS!



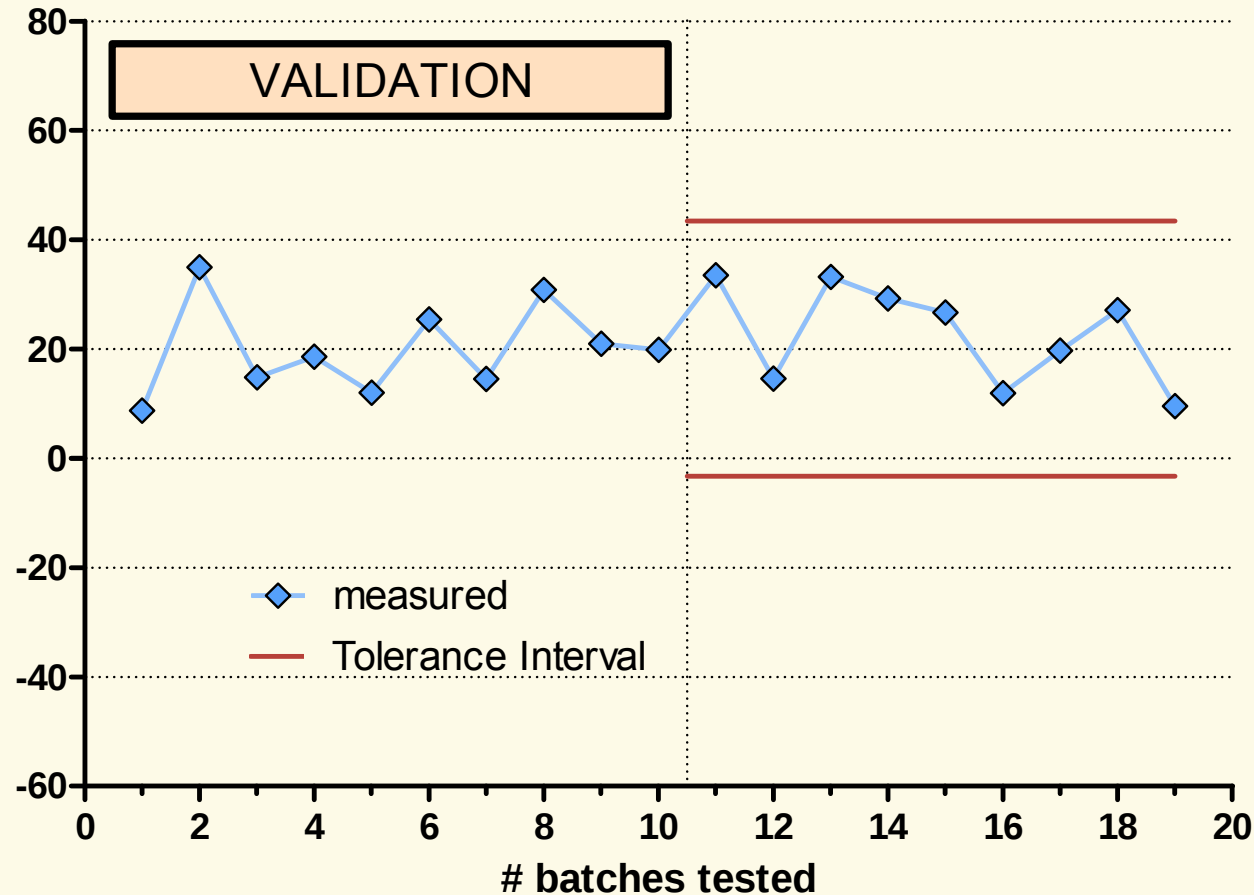
Dynamic Tolerance Intervals

TI widens, when data shows a trend – may lead to undesired effects

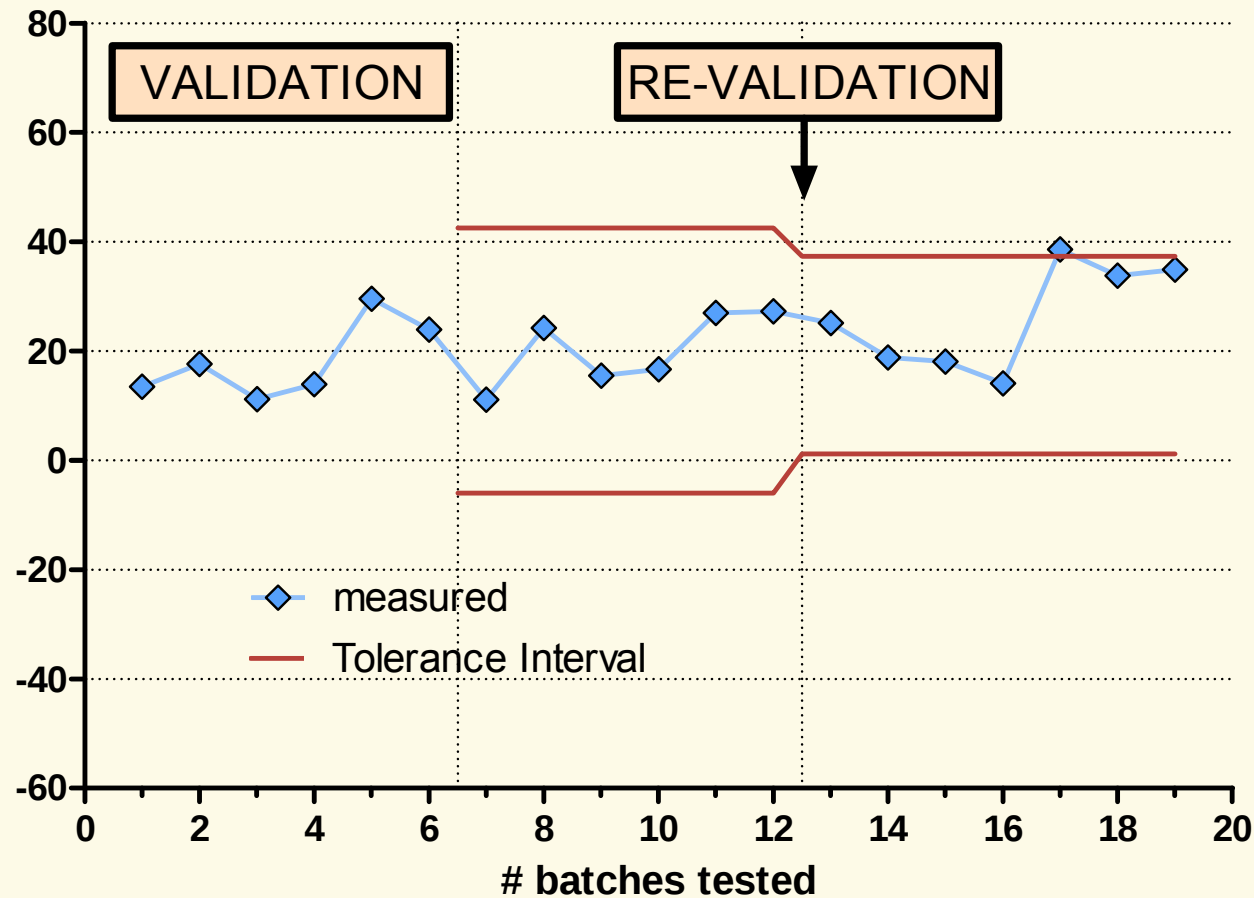


Fixed Tolerance Intervals

With a sufficient amount of validation data the TI will be more reliable



Two-Step Approach



Process performance indices, 6 sigmas, ...

- PPI: Similar to reference limits (mean $\pm$ 3SD x Ppu)
- Advantage to be product specific
- BUT: Wouldn't such limits be too wide (and could include e.g. OOS batches)?
- At least: Limits must exclude range, where sub-potency, non-safety, ... starts
- Thus: 6 sigmas are not recommended (for normal or similar distributed data these would include anything)

Summary

Crucial: Reliable estimation of the specification limits

- Too narrow intervals could result in too many re-tests and / or falsely rejected batches
- Too wide intervals could lead to falsely released batches (sub-potent, safety concerns, ...)
- Specification based on what we have observed so far (might be few), thus future results may represent what we missed in validation
- Samples used for validation were too homogeneous (too narrow specifications) – bad luck?
- Samples used for validation had high variability (new processes, untrained personnel, too wide specifications)
- Validation performed with few samples, repeatedly tested (should be avoided!)

Summary II

- For a complete new product it will be difficult to set up reliable specification limits with only 3 batches/tests
 - risk of miss-specification might be high, especially if variability of parameter of interest is expected to be high; a re-validation should be planned (n=8-12 batches) → 2-step-approach
- No universal tool available – parameter / product dependent
 - Aim to obtain high sensitivity to detect critical batches (sub-potent, safety risks, ...) and
 - To obtain high specificity in order to avoid false negative results and to limit unnecessary re-tests

Thank you for your attention

